

18.06

Professor Strang

Quiz 1

October 4, 2006

Grading

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Your PRINTED name is: _____

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Please circle your recitation:

- 1) T 10 2-131 K. Meszaros 2-333 3-7826 karola
- 2) T 10 2-132 A. Barakat 2-172 3-4470 barakat
- 3) T 11 2-132 A. Barakat 2-172 3-4470 barakat
- 4) T 11 2-131 A. Osorno 2-229 3-1589 aosorno
- 5) T 12 2-132 A. Edelman 2-343 3-7770 edelman
- 6) T 12 2-131 K. Meszaros 2-333 3-7826 karola
- 7) T 1 2-132 A. Edelman 2-343 3-7770 edelman
- 8) T 2 2-132 J. Burns 2-333 3-7826 burns
- 9) T 3 2-132 A. Osorno 2-229 3-1589 aosorno

1 (24 pts.) This question is about an m by n matrix A for which

$$Ax = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} \text{ has no solutions} \quad \text{and} \quad Ax = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \text{ has exactly one solution.}$$

- (a) Give all possible information about m and n and the rank r of A .
- (b) Find all solutions to $Ax = 0$ and **explain your answer**.
- (c) Write down an example of a matrix A that fits the description in part (a).

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2 (24 pts.) The 3 by 3 matrix A reduces to the identity matrix I by the following three row operations (in order):

E_{21} : Subtract 4 (row 1) from row 2.

E_{31} : Subtract 3 (row 1) from row 3.

E_{23} : Subtract row 3 from row 2.

- (a) Write the inverse matrix A^{-1} in terms of the E 's. **Then compute A^{-1} .**
- (b) What is the original matrix A ?
- (c) What is the lower triangular factor L in $A = LU$?

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3 (28 pts.) This 3 by 4 matrix depends on c :

$$A = \begin{bmatrix} 1 & 1 & 2 & 4 \\ 3 & c & 2 & 8 \\ 0 & 0 & 2 & 2 \end{bmatrix}$$

(a) *For each c* find a basis for the column space of A .

(b) *For each c* find a basis for the nullspace of A .

(c) *For each c* find the complete solution x to $Ax = \begin{bmatrix} 1 \\ c \\ 0 \end{bmatrix}$.

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- 4 (24 pts.) (a) If A is a 3 by 5 matrix, what information do you have about the nullspace of A ?
- (b) Suppose row operations on A lead to this matrix $R = \text{rref}(A)$:

$$R = \begin{bmatrix} 1 & 4 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

Write all known information about the columns of A .

- (c) In the vector space M of all 3 by 3 matrices (you could call this a matrix space), what subspace S is spanned by all possible row reduced echelon forms R ?

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